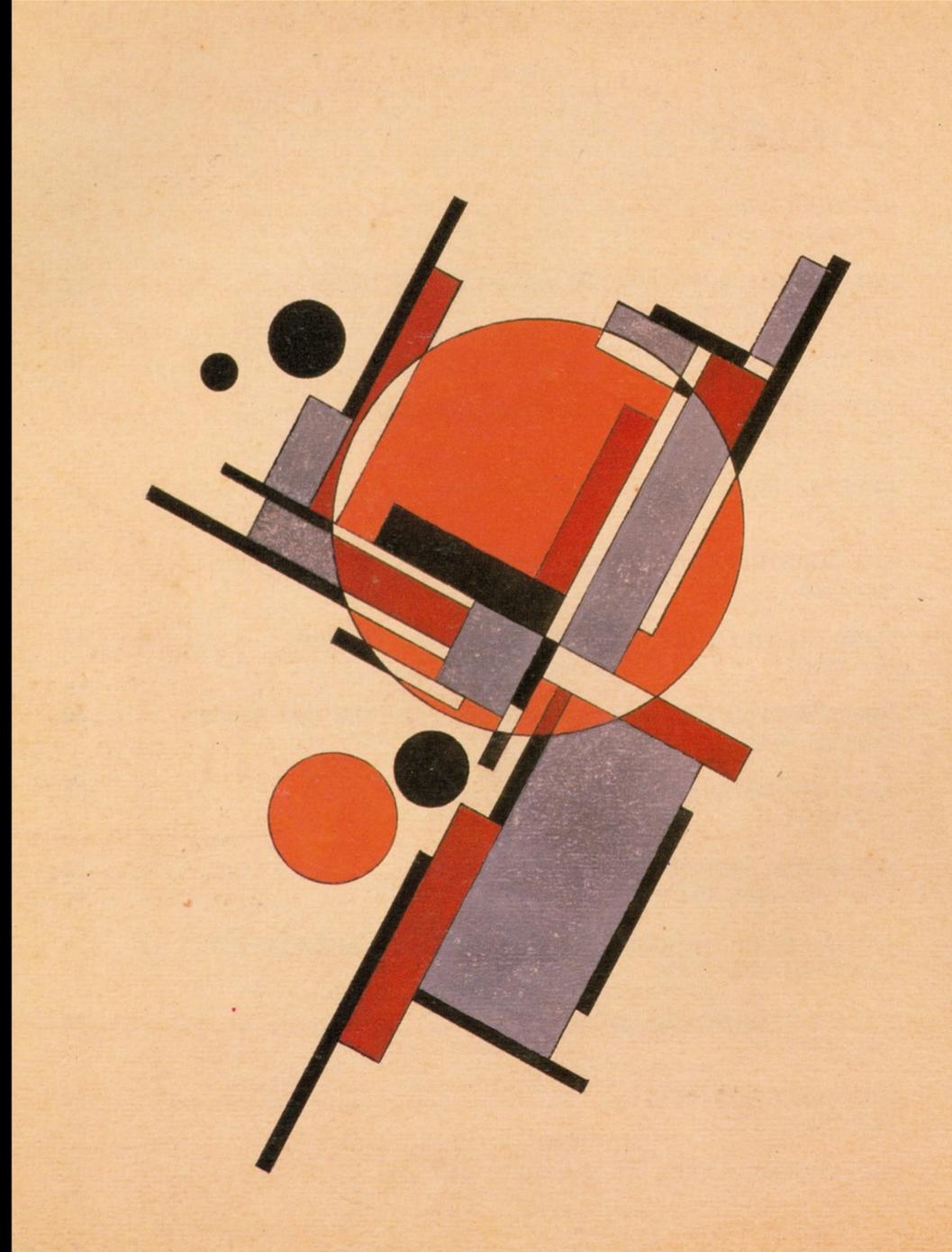


Superconducting qubits

State-of-the-art and where do we go from here?



Danish Quantum Community Conference
Oct 7th 2020
Morten Kjaergaard



Postdoctoral associate
Engineering Quantum Systems
Massachusetts Institute of Technology

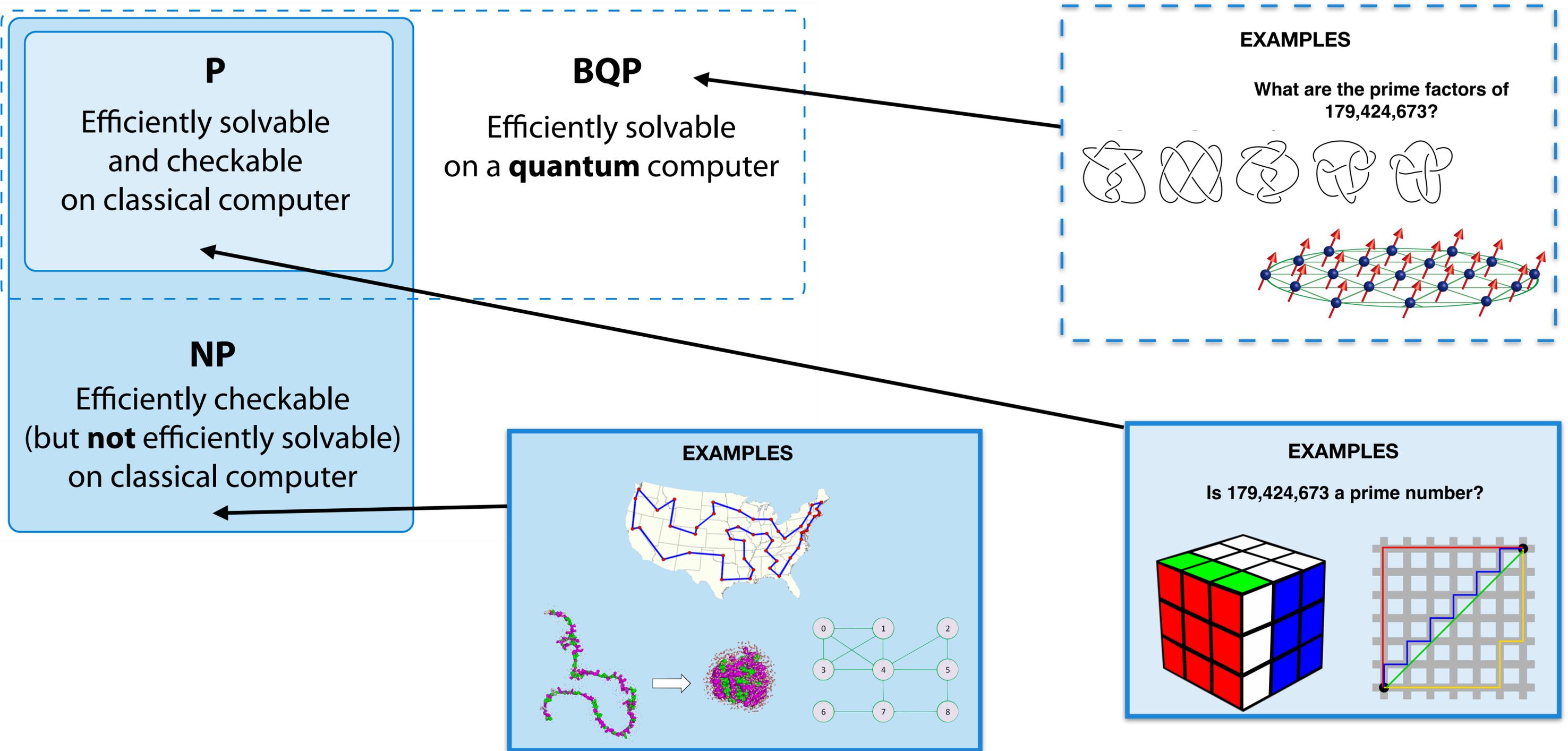


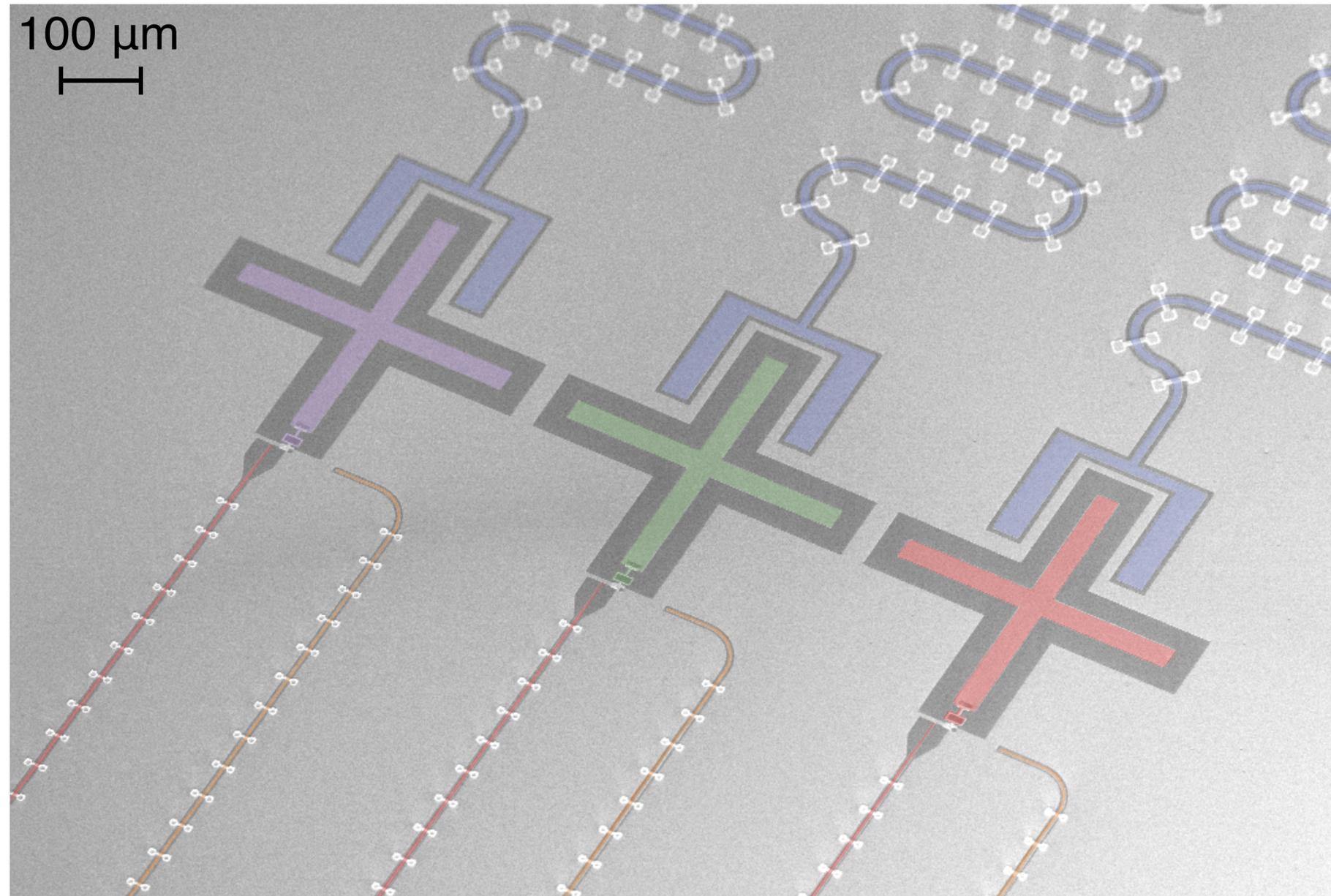
Center for
Quantum
Devices



(starting Nov 2020)
Assistant Professor
Center for Quantum Devices
University of Copenhagen

Computations using quantum bits (*performed in a highly specific way*) can provide computational speedups (*for certain problems*)

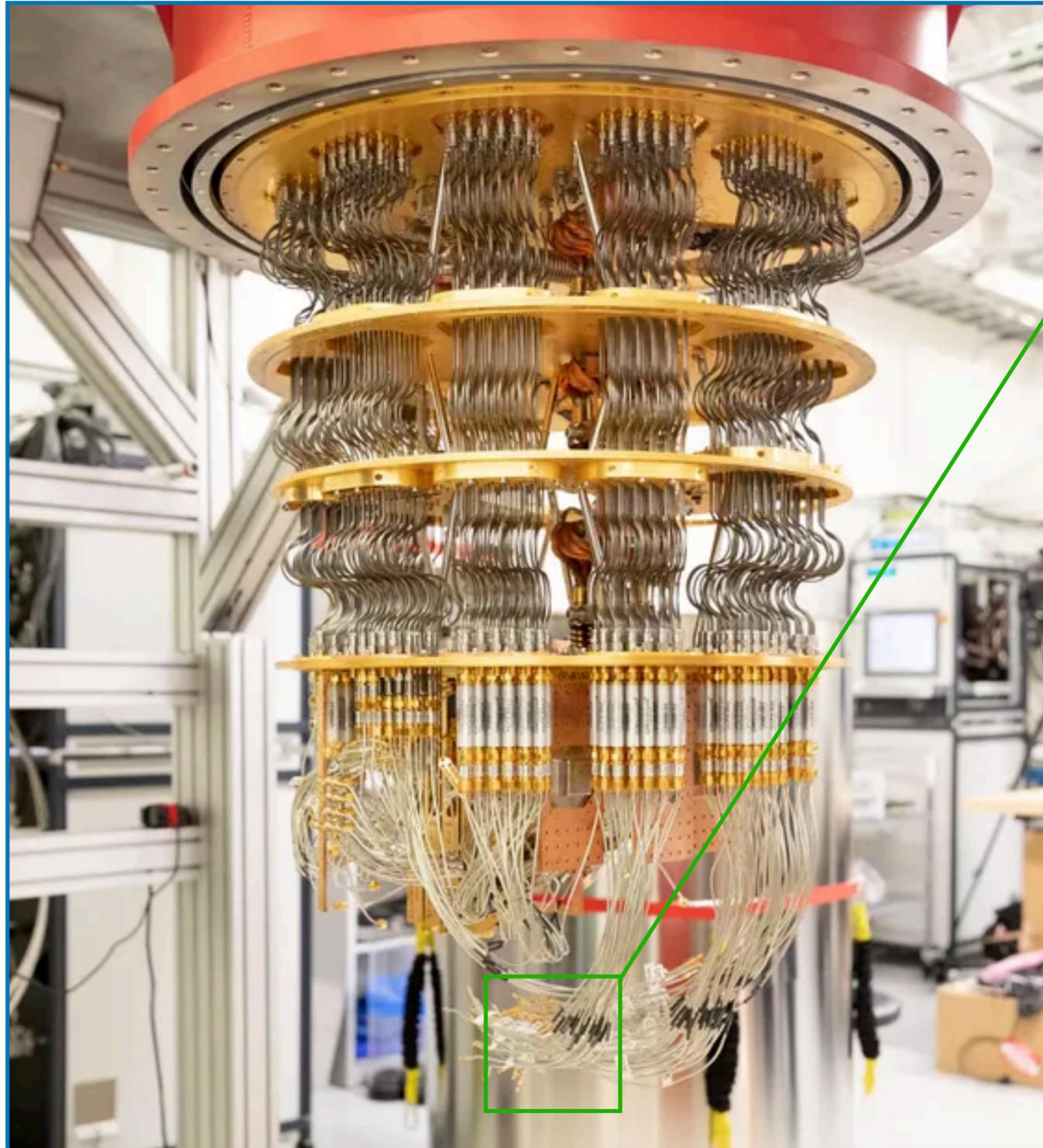




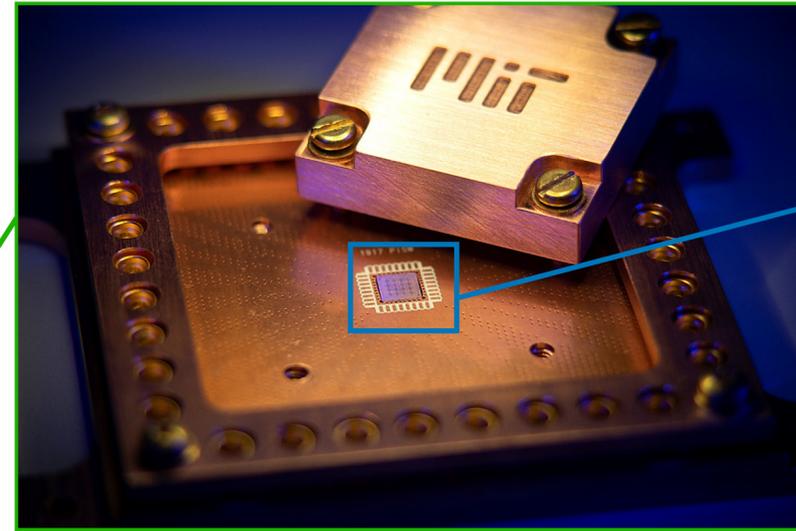
Electrical circuits fabricated using superconducting materials and patterned with nano- and microlithography techniques:

- *Quantum* properties can be changed, just by changing electrical pattern
- *Exceedingly* reproducible -> can be prototyped and optimized very quickly

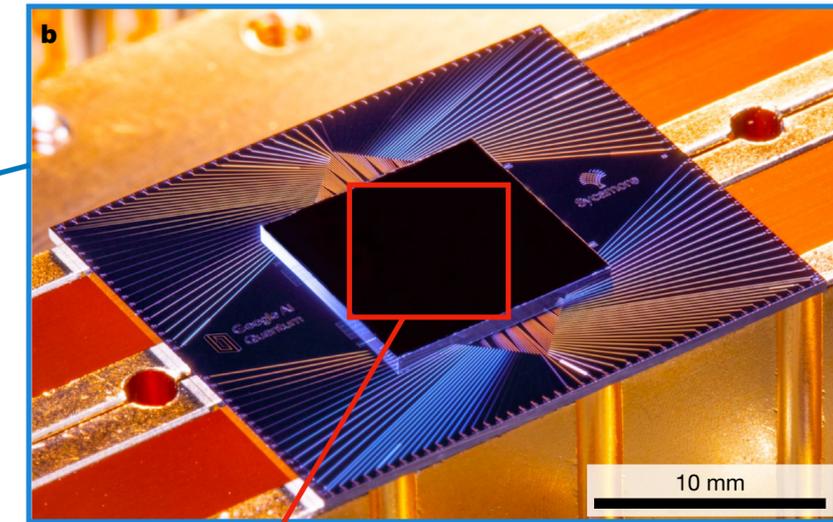
Google Quantum AI



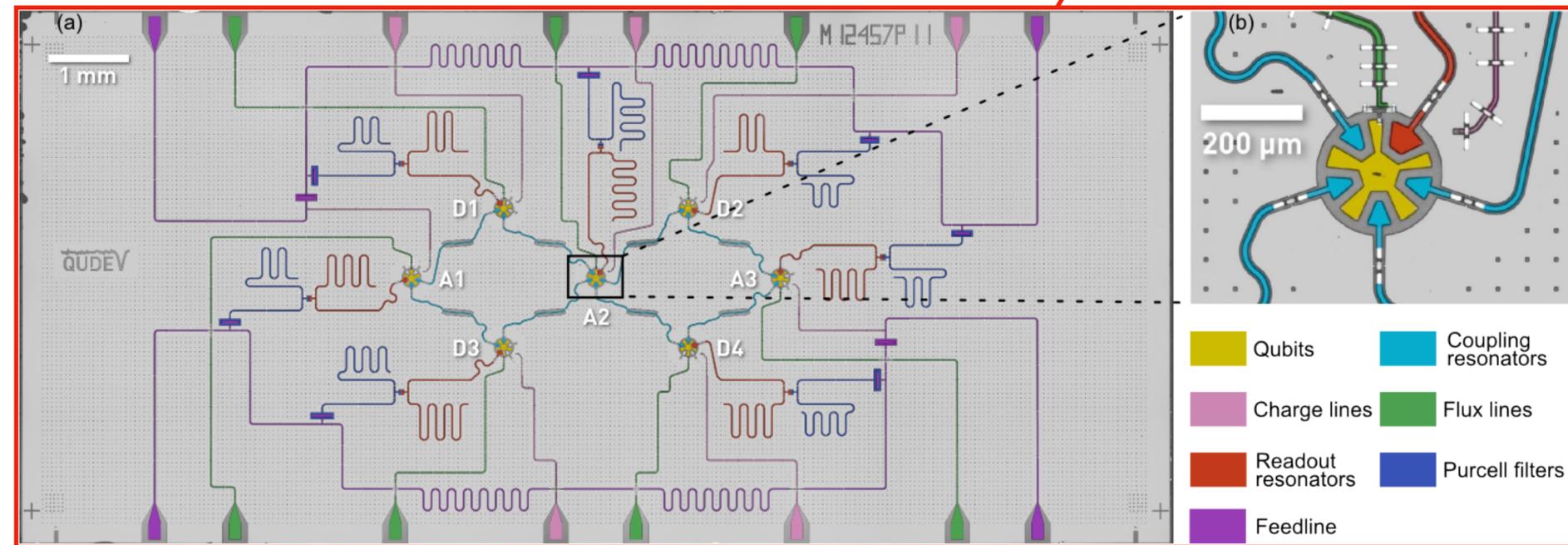
EQuS (MIT)



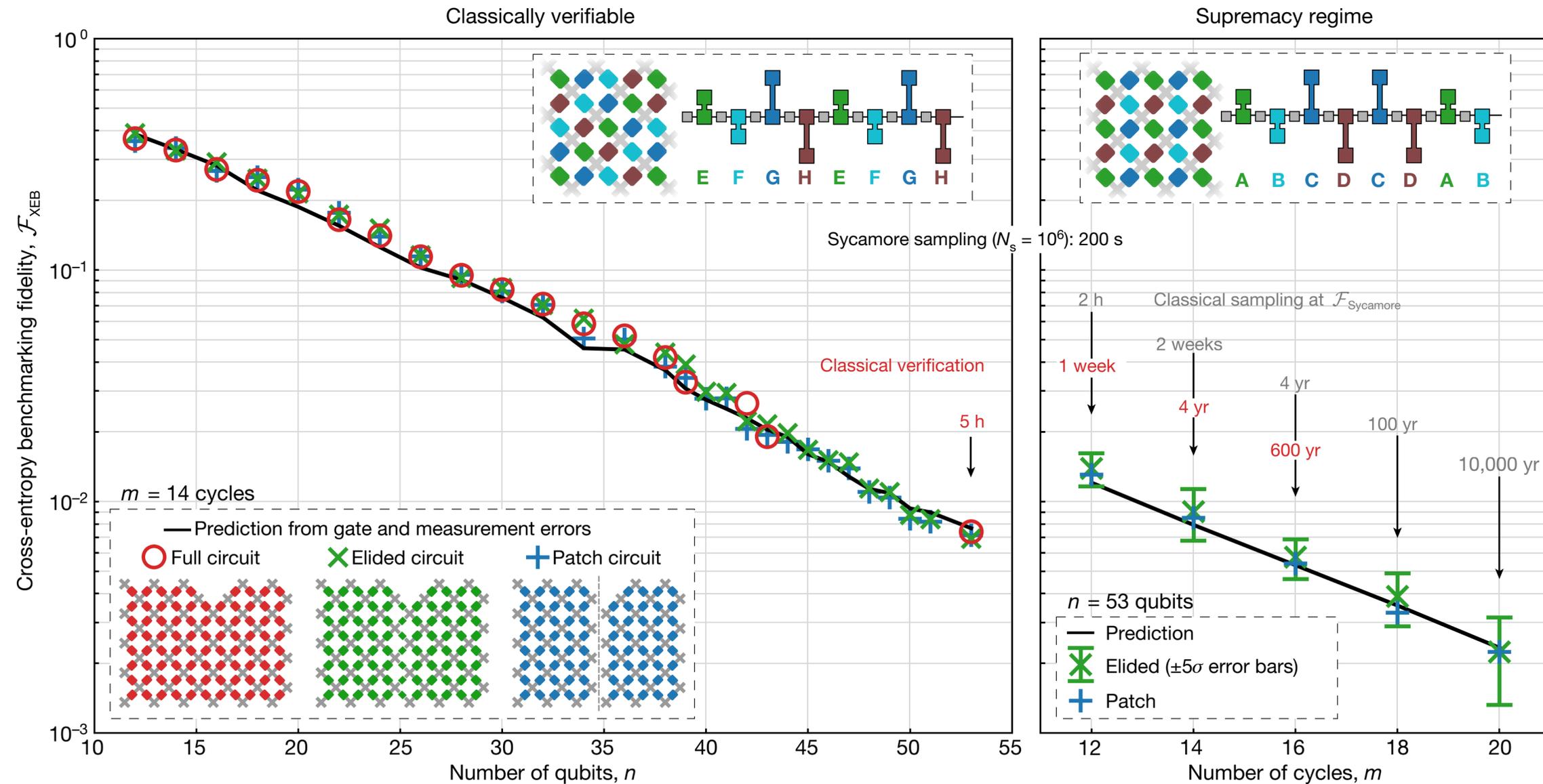
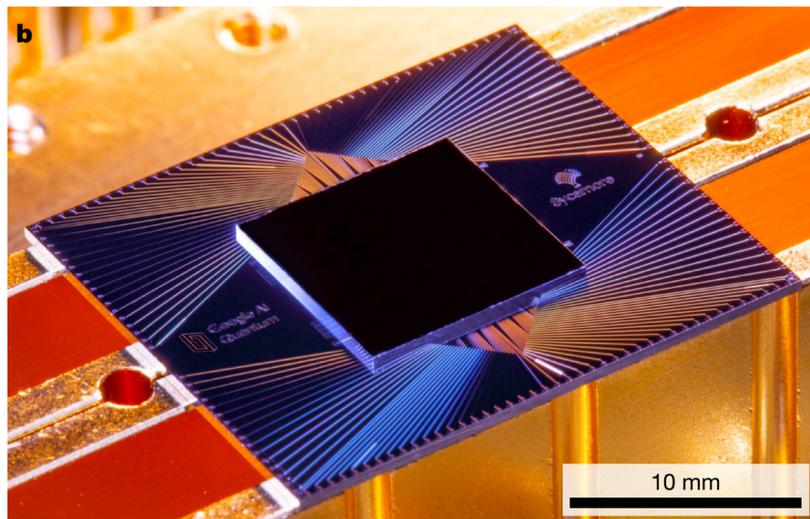
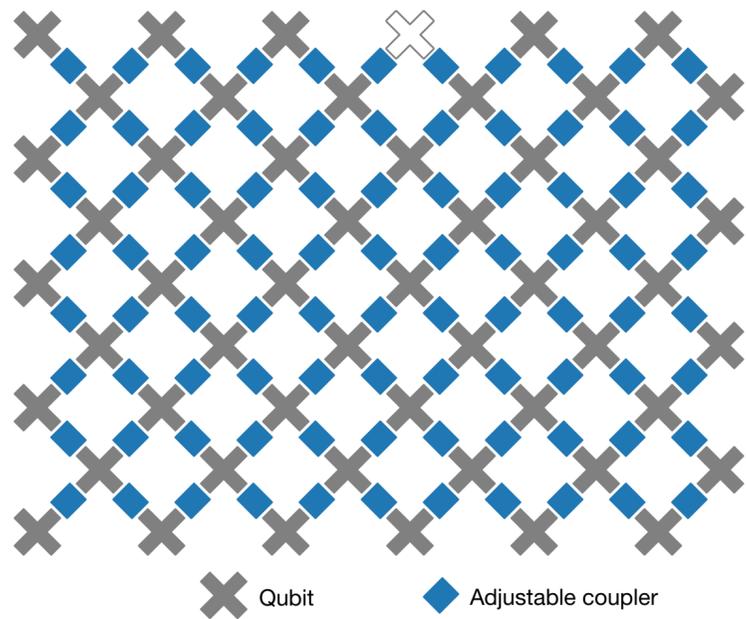
Google Quantum AI



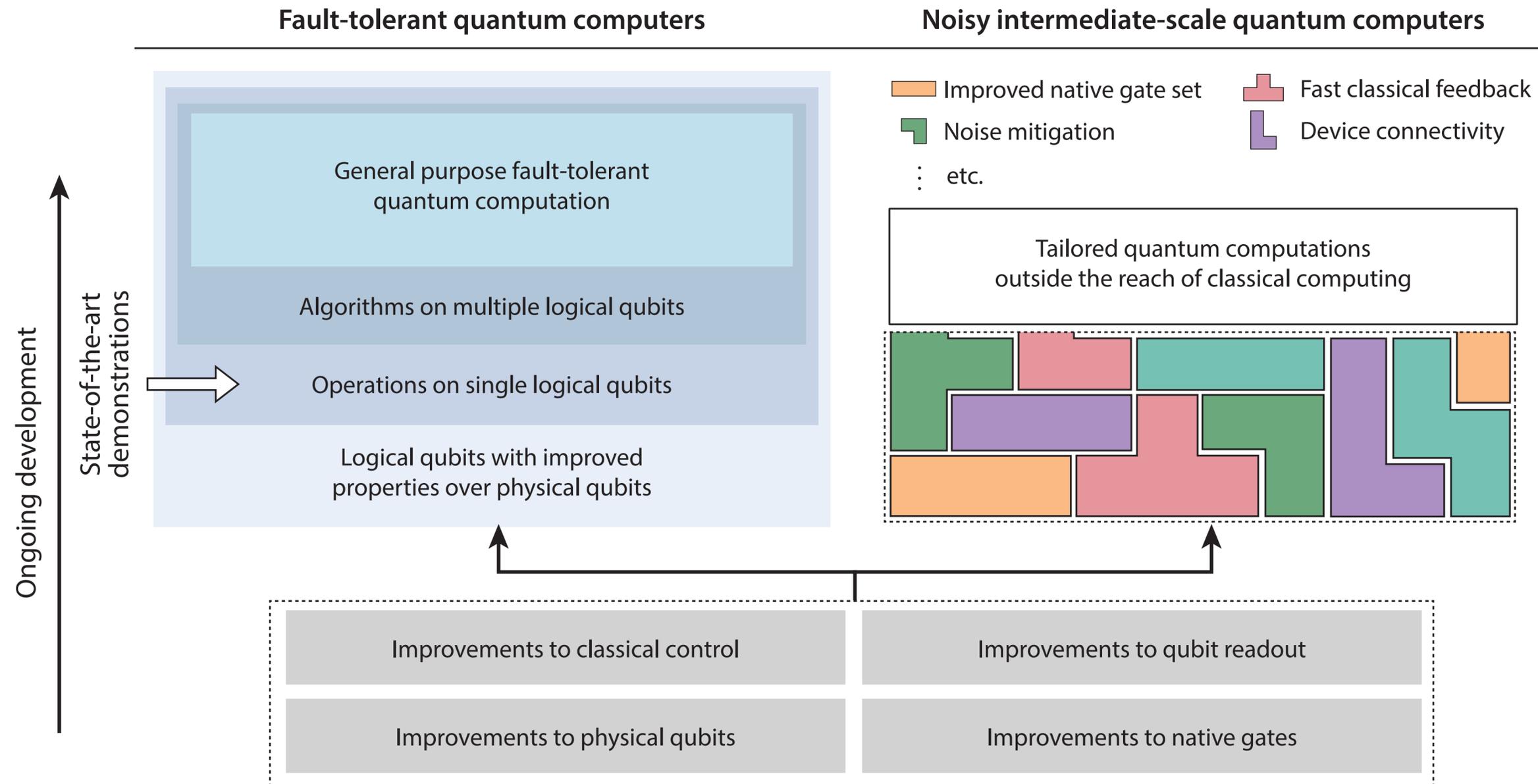
Wallraff Group (ETH Zurich)



Late last year a *superconducting* quantum computer outperformed the worlds largest classical supercomputer:



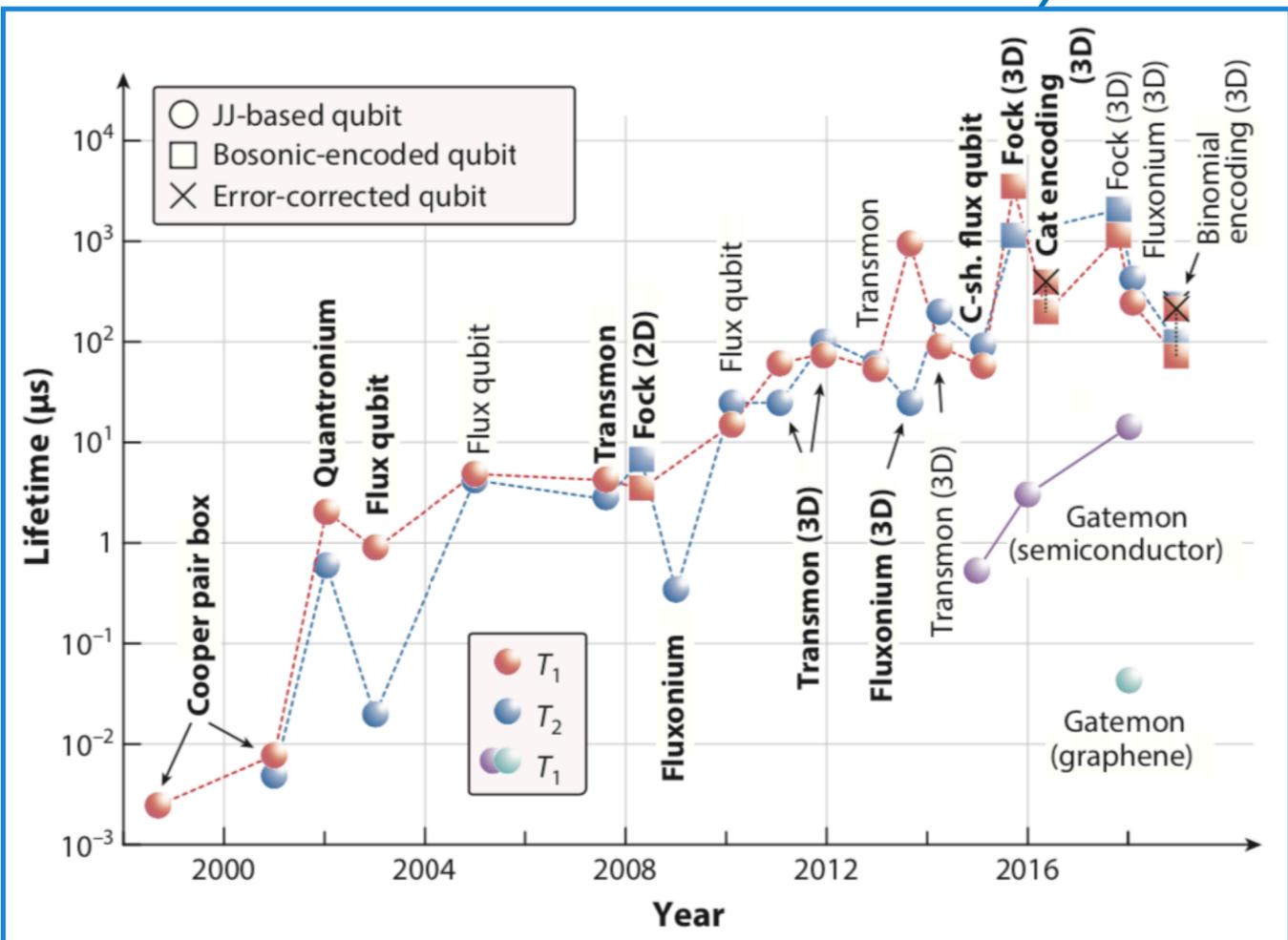
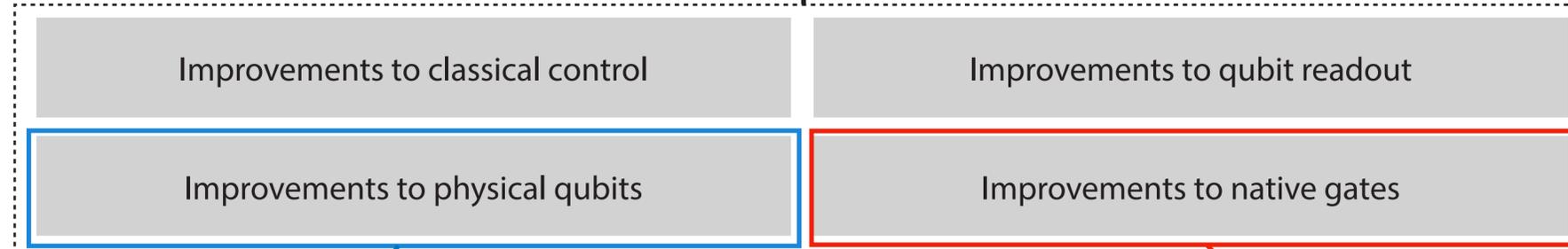
Using 53 superconducting qubit (of the *transmon* variety), the Google Quantum AI team demonstrated a calculation in ~200s that is expected to take between ~a few weeks and up to ~10.000 years on the Summit supercomputer





Superconducting quantum computing: Where are we going?

Ongoing



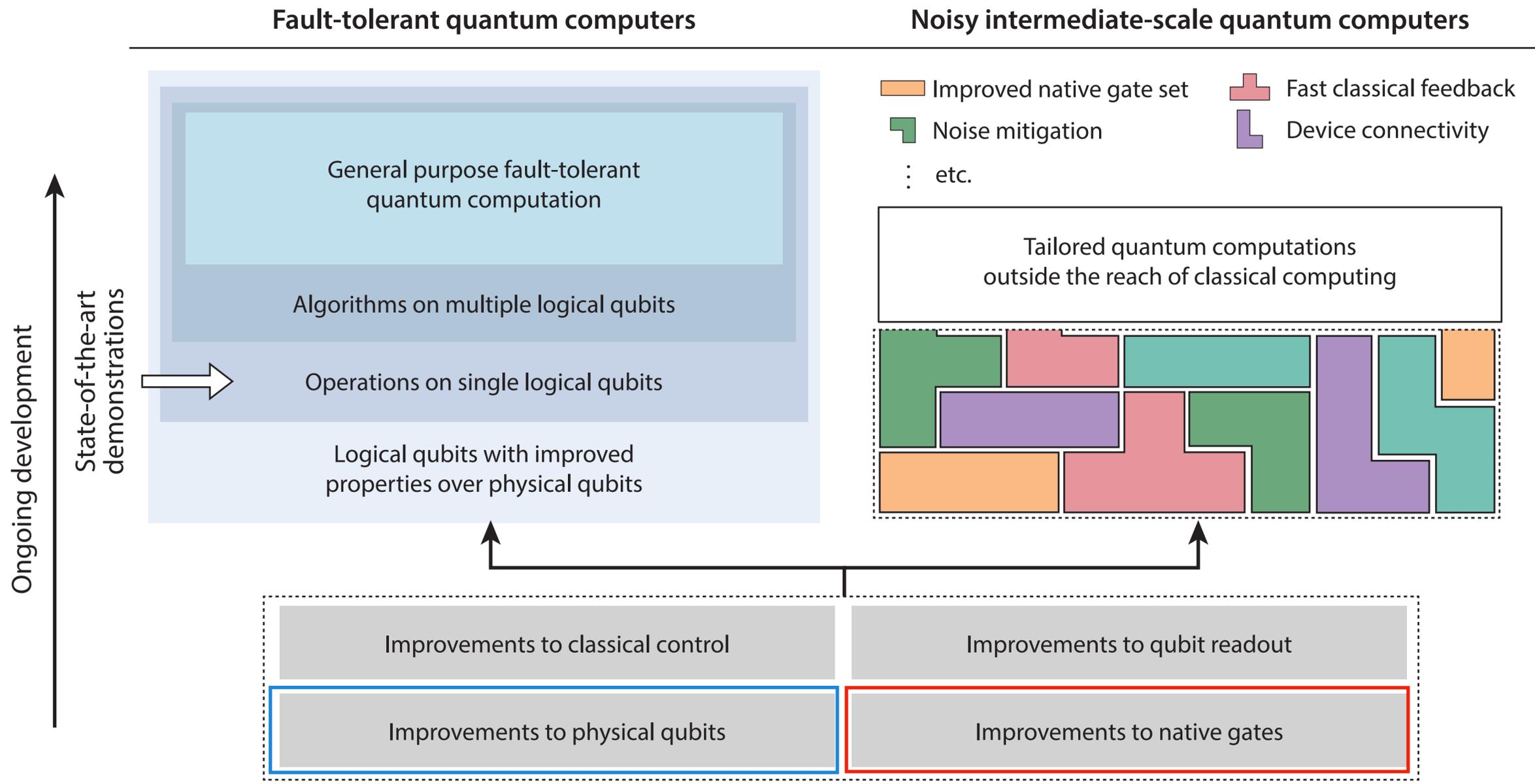
‘Lifetime’ is approximately the time for which the qubit ‘retains its memory’. *Key metric.*

Table 1 State-of-the-art high-fidelity, two-qubit gates in superconducting qubits^a

Acronym ^b	Layout ^c	First demonstration [Year]	Highest fidelity [Year]	Gate time
CZ (ad.)	T-T	DiCarlo et al. (72) [2009]	99.4% ^e Barends et al. (3) [2014]	40 ns
			99.7% ^e Kjaergaard et al. (73) [2020]	60 ns
\sqrt{i} SWAP	T-T	Neeley et al. (81) ^d [2010]	90% ^g Dewes et al. (74) [2014]	31 ns
CR	F-F	Chow et al. (75) ^h [2011]	99.1% ^e Sheldon et al. (5) [2016]	160 ns
\sqrt{b} SWAP	F-F	Poletto et al. (76) [2012]	86% ^g Poletto et al. (76) [2012]	800 ns
MAP	F-F	Chow et al. (77) [2013]	87.2% ^g Chow et al. (75) [2011]	510 ns
CZ (ad.)	T-(T)-T	Chen et al. (55) [2014]	99.0% ^e Chen et al. (55) [2014]	30 ns
RIP	3D F	Paik et al. (78) [2016]	98.5% ^e Paik et al. (78) [2016]	413 ns
\sqrt{i} SWAP	F-(T)-F	McKay et al. (79) [2016]	98.2% ^e McKay et al. (79) [2016]	183 ns
CZ (ad.)	T-F	Caldwell et al. (80) [2018]	99.2% ^e Hong et al. (6) [2019]	176 ns
CNOT _L	BEQ-BEQ	Rosenblum et al. (13) [2018]	~99% ^f Rosenblum et al. (13) [2018]	190 ns
CNOT _{T-L}	BEQ-BEQ	Chou et al. (82) [2018]	79% ^g Chou et al. (82) [2018]	4.6 μ s

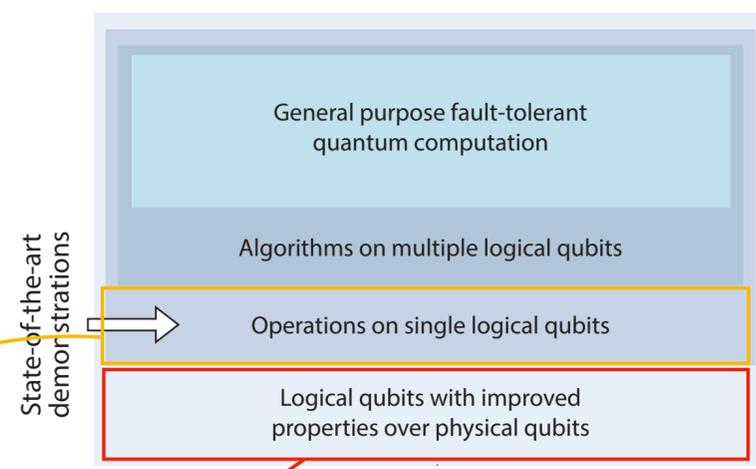
‘Fidelity’ is approximately the ‘quality’ of the quantum operation that generates *entanglement* in the quantum processor. *Key metric.*

$$\text{operation count} = \frac{T_2 \text{ lifetime}}{\text{gate time}}$$

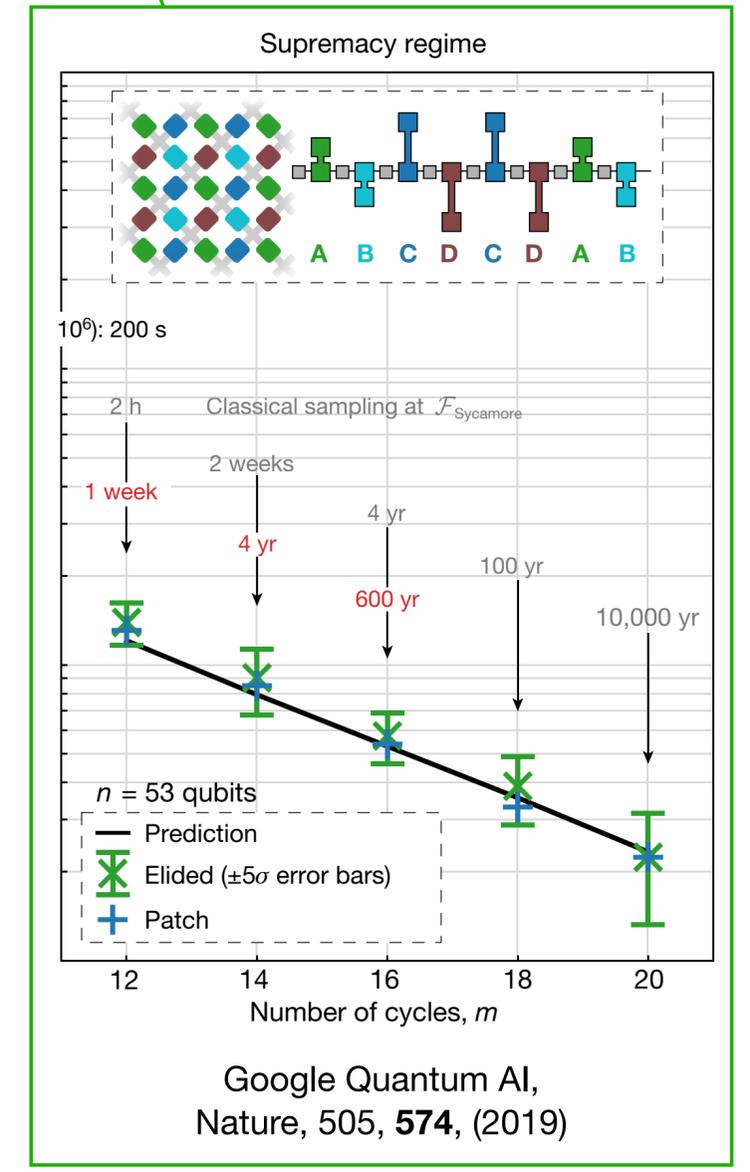
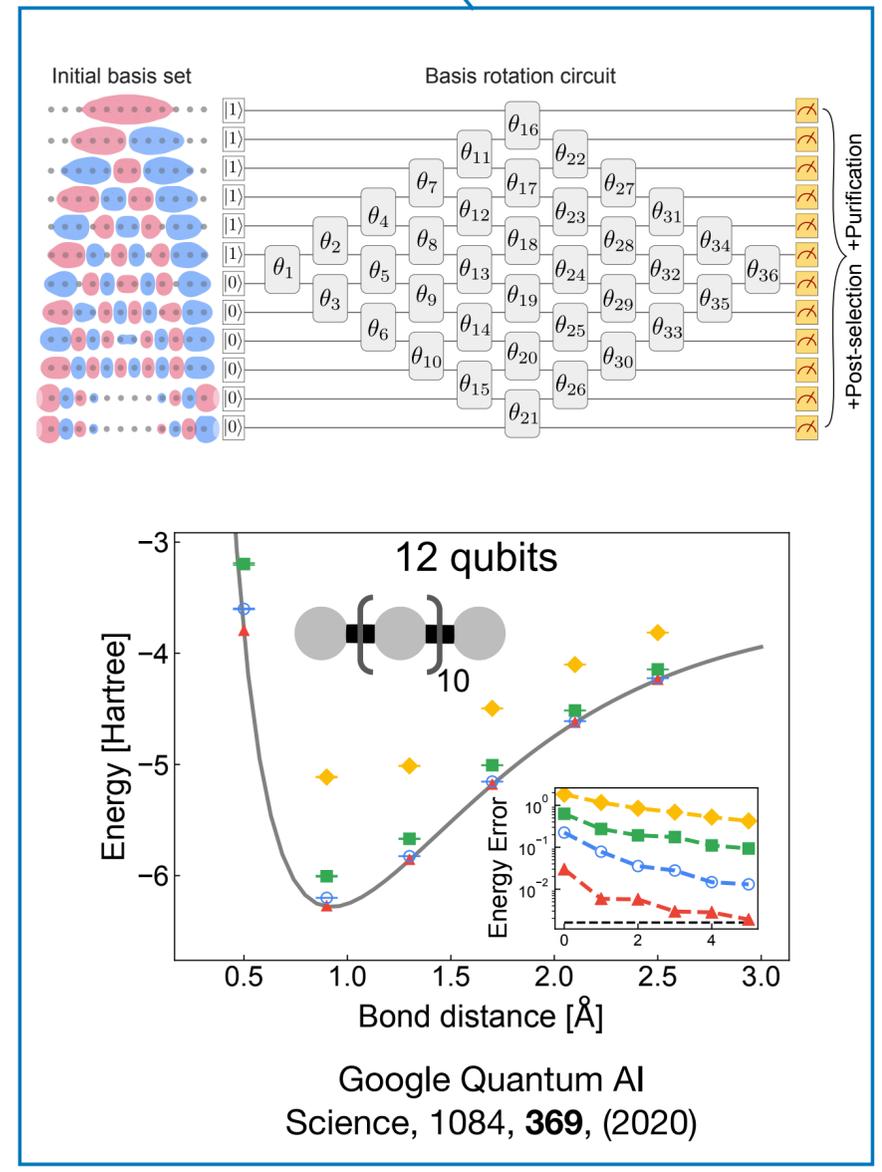
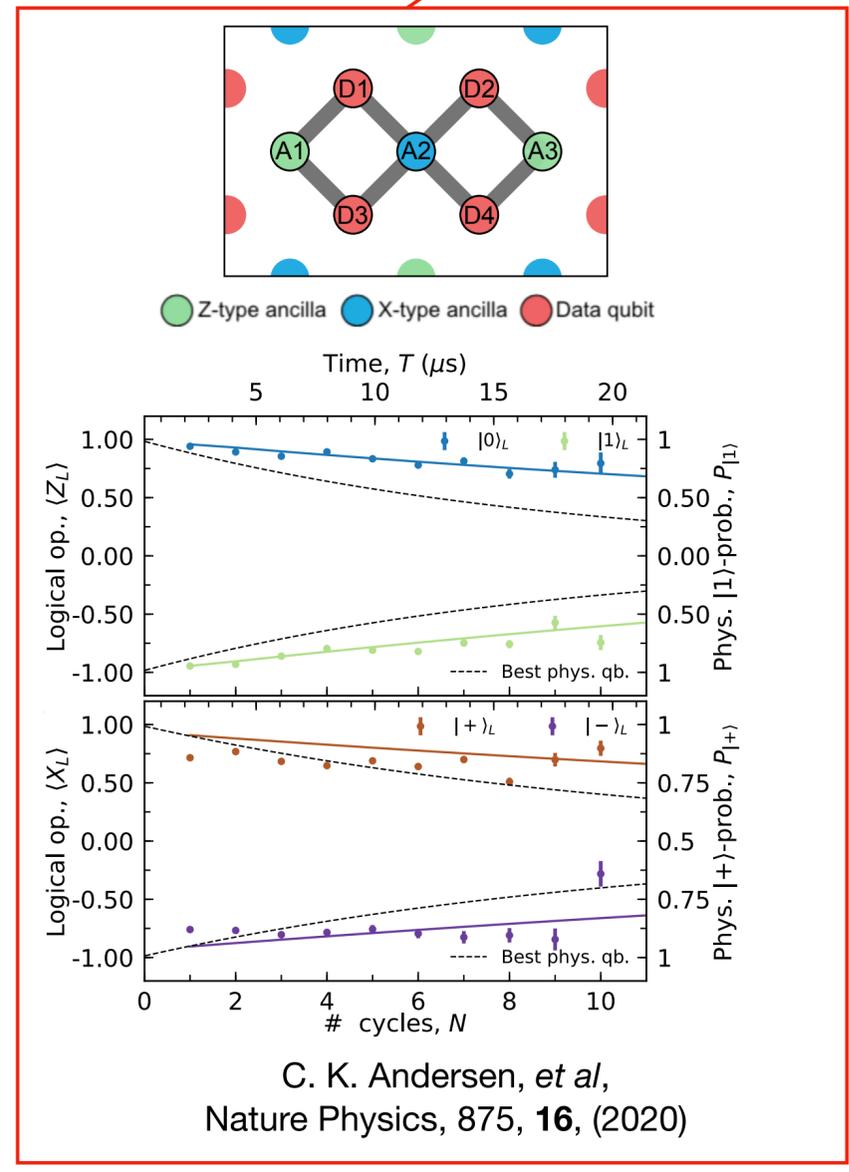
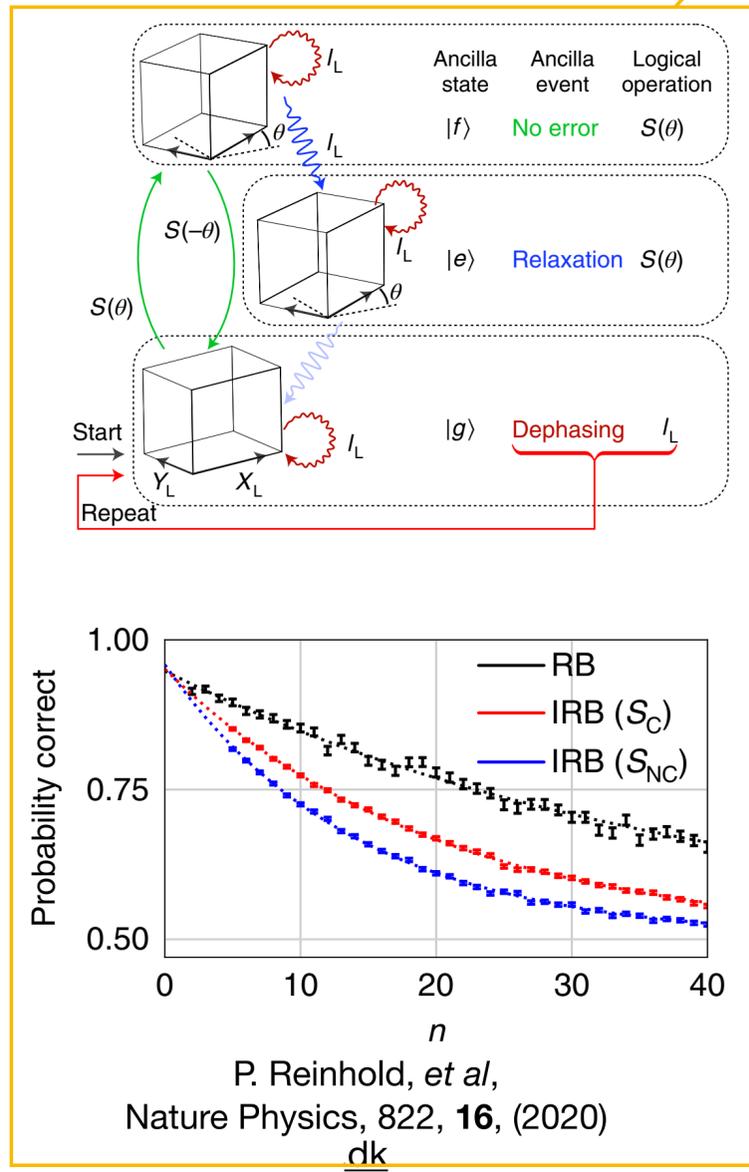
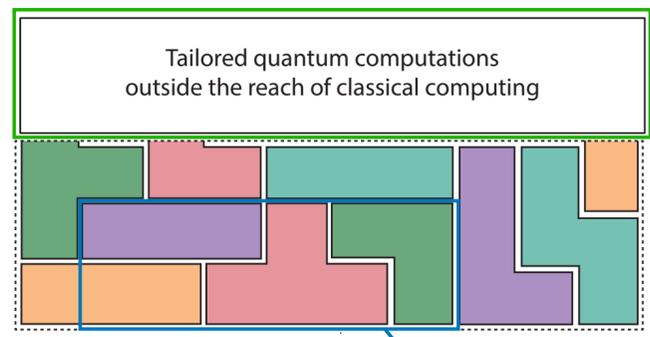


Fault-tolerant quantum computers

Noisy intermediate-scale quantum computers

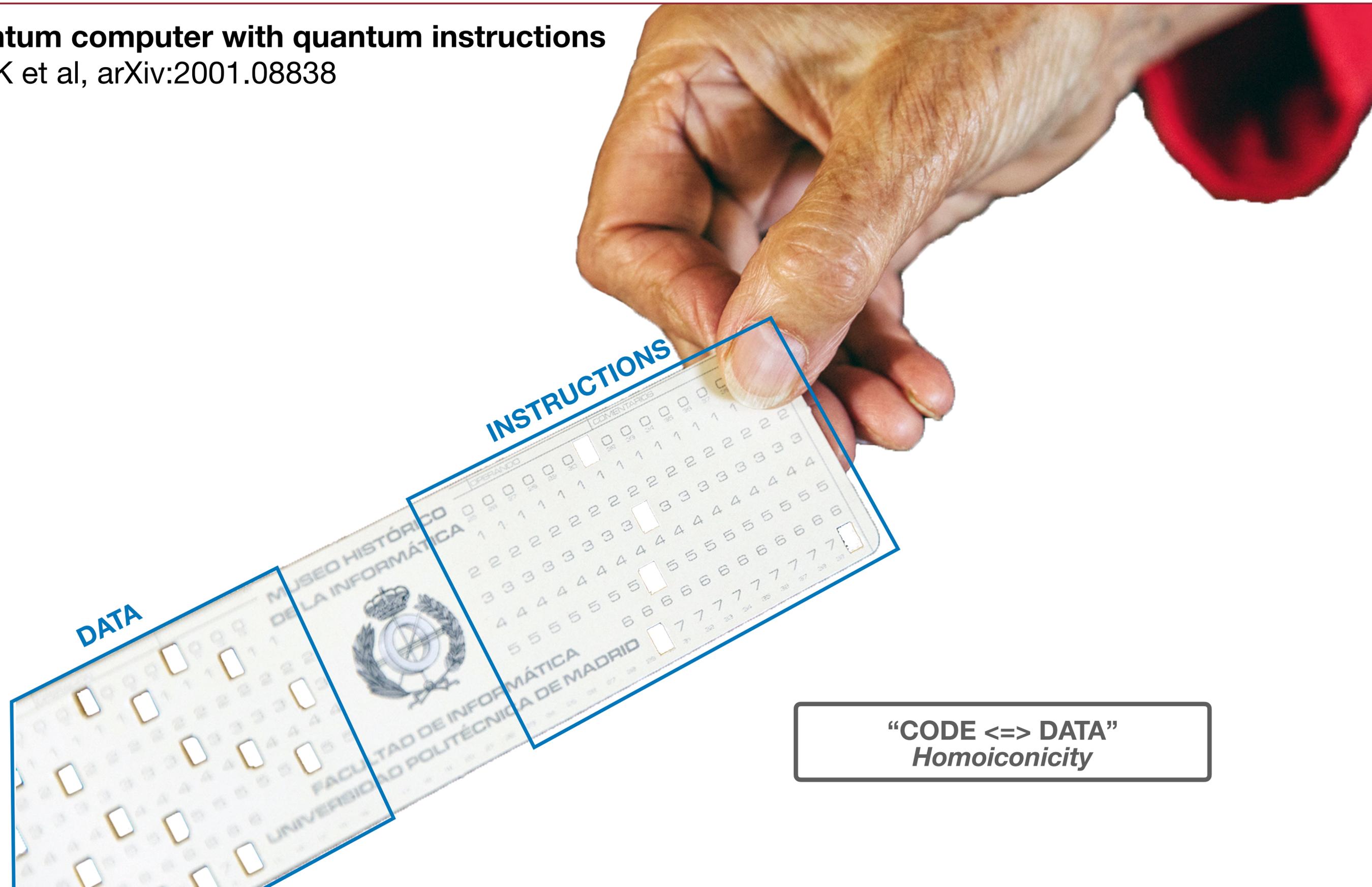


- Improved native gate set
- Noise mitigation
- etc.
- Fast classical feedback
- Device connectivity



Programming a quantum computer with quantum instructions

MK et al, arXiv:2001.08838

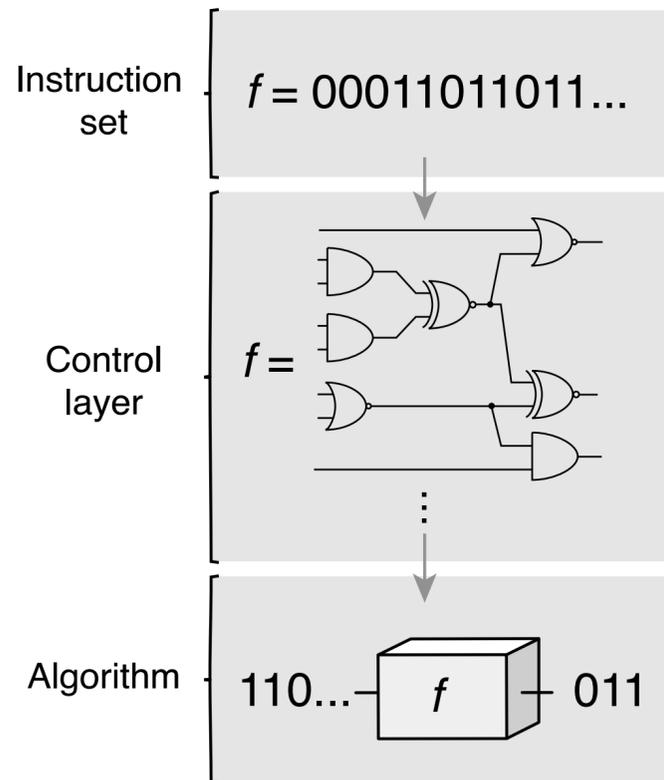


“CODE \Leftrightarrow DATA”
Homoiconicity

“CODE \Leftrightarrow DATA”

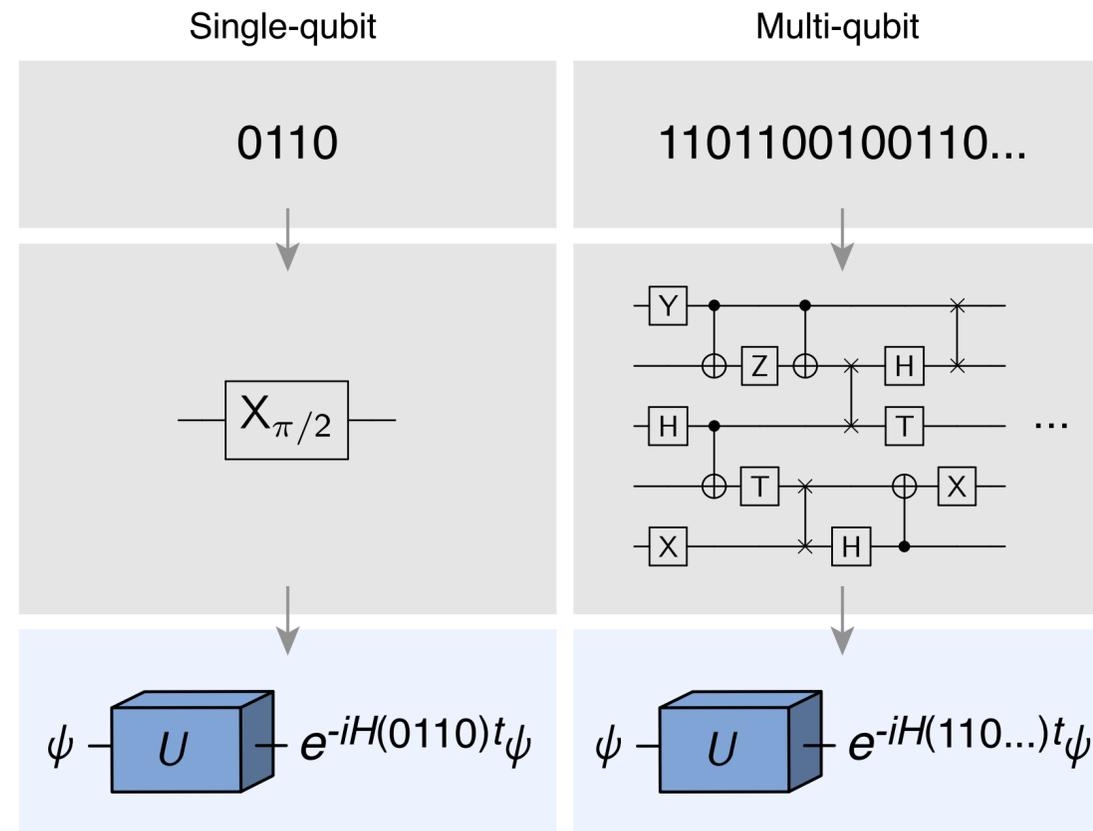
CODE: CLASSICAL
DATA: CLASSICAL

Classical instruction set for classical computing



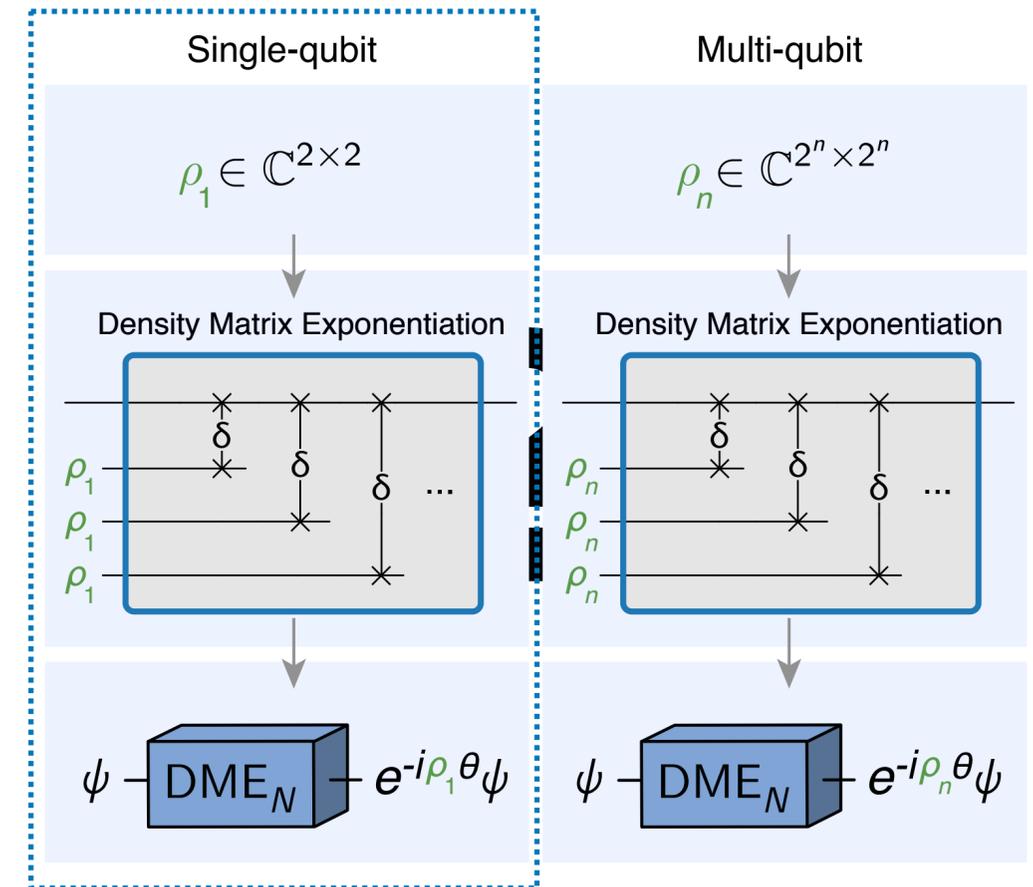
CODE: CLASSICAL
DATA: QUANTUM

Classical instruction set for quantum computing



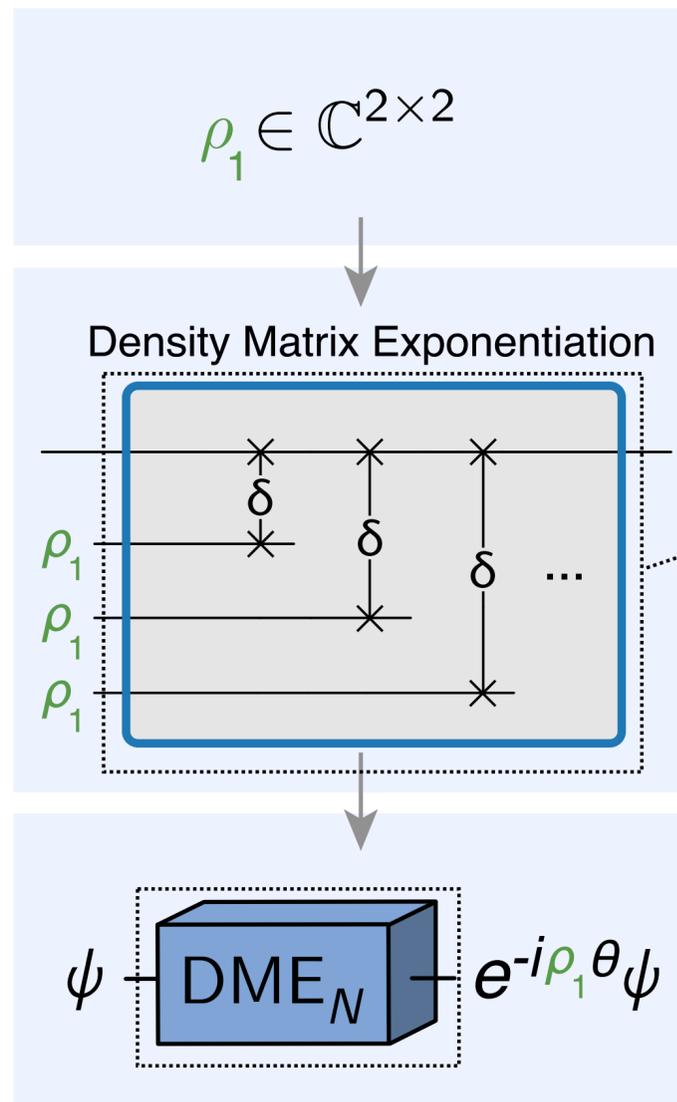
CODE: QUANTUM
DATA: QUANTUM

Quantum instruction set for quantum computing



Rest of this talk

- Classical computing
- Quantum computing



DME is a fixed protocol that implements an operation only dependent on the setting of the instruction state ρ :

$$\rho^{\otimes N} \xrightarrow{\text{DME}_N} e^{-i\rho\theta} + \mathcal{O}(\theta^2/N)$$

(θ an angle)

Seth Lloyd *et al*, Nat. Phys. 2014

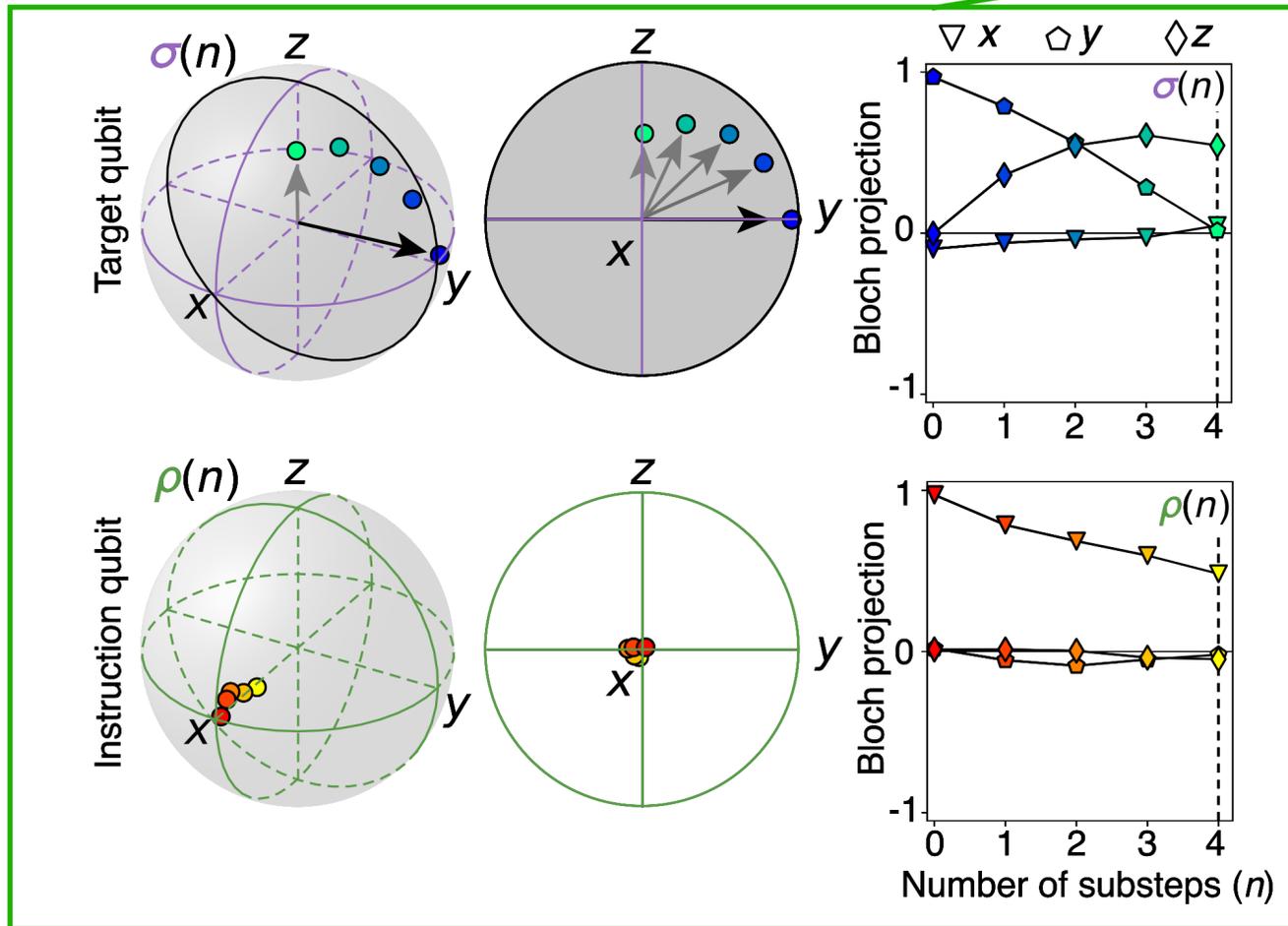
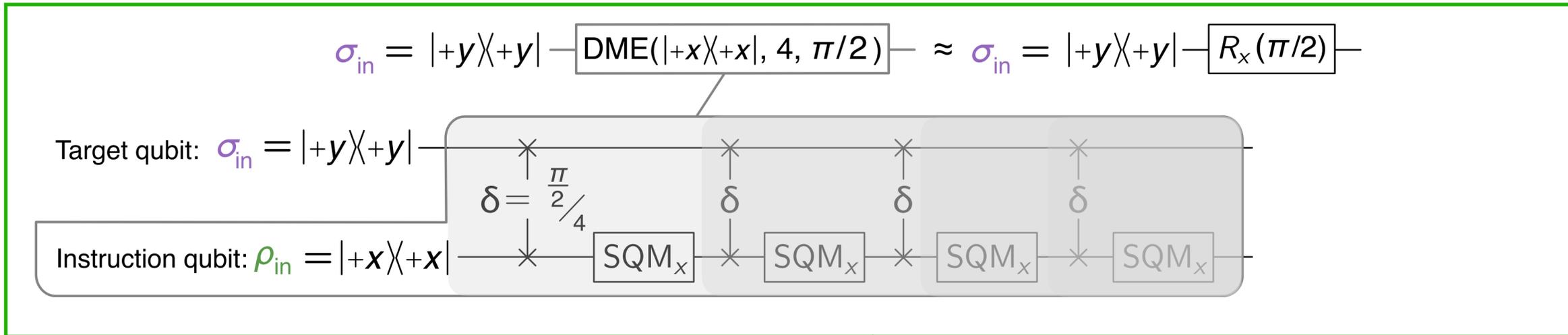
Conceptually

Density Matrix Exponentiation allows us to load a program into a state ('instruction state' or 'quantum program', ρ) and execute that quantum program on another quantum system

$$\sigma_{in} = |+_y\rangle\langle+_y| - \boxed{\text{DME}(|+_x\rangle\langle+_x|, 4, \pi/2)} - \approx \sigma_{in} = |+_y\rangle\langle+_y| - \boxed{R_x(\pi/2)} -$$

Instruction state
Total angle θ

Number of steps N



Single qubit DME

Instruction state: $\rho = | +x \rangle \langle +x |$:

$$\rho = | +x \rangle \langle +x | = \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix} = \frac{1}{2} (\mathbb{1} + \sigma_x)$$

Input to density matrix exponentiation:

$$e^{-i\rho\theta} = e^{-i\frac{1}{2}(\mathbb{1} + \sigma_x)\theta} \simeq e^{-i\sigma_x\frac{\theta}{2}} = R_x(\theta)$$

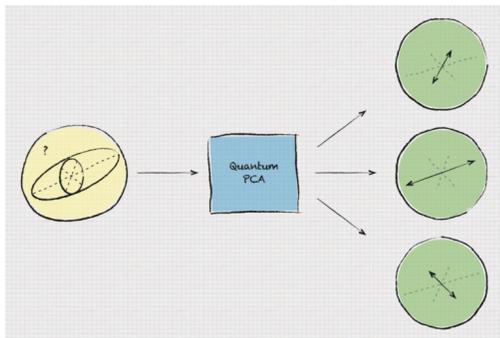
The setting of the instruction qubit “instructs” axis to rotate the target qubit about

DME is exceedingly efficient for generating quantum instructions

Exponential reduction in resource requirements over *any* tomographic strategy
(Kimmel *et al*, npj QI 2017)

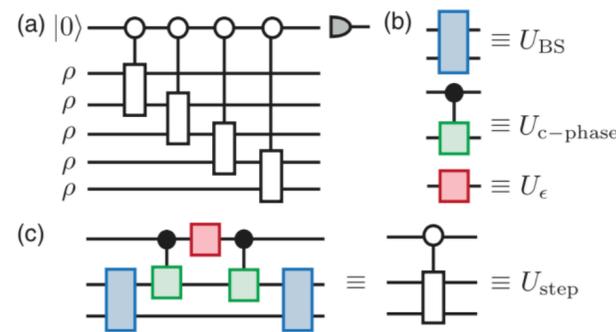
Algorithm runtime scales only logarithmically with dimension of instruction state
(Lloyd *et al*, Nat. Phys. 2014, Marvian & Lloyd (2016), Kimmel *et al*, npj QI 2017)

Quantum principal component analysis



Lloyd *et al*, Nat. Phys., **10** 631 (2014)

Efficient measurements of entanglement spectra



Pichler *et al*, PRX, **6** 041033 (2016)

Sample optimal Hamiltonian simulation

Theorem 2 Let $f(t, \delta)$ be the number of copies of ρ required to implement the unitary $e^{-i\rho t}$ up to error δ in trace norm. Then as long as $\delta \leq 1/6$ and $\delta/t \leq 1/(6\pi)$, it holds that $f(t, \delta) = \Theta(t^2/\delta)$.

Kimmel *et al*, npj QI, **3** 13 (2017)

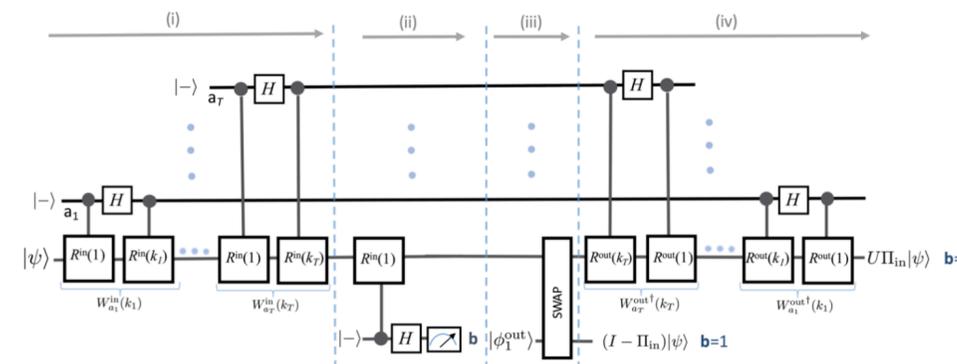
Quantum semi-definite programming

Algorithm 5: Efficiently testing the feasibility of SDPs: Quantum input model.

- 1 Initialize the weight matrix $W^{(1)} = I_n$, and $T = \frac{16 \ln n}{\epsilon^2}$;
- 2 **for** $t = 1, 2, \dots, T$ **do**
- 3 Prepare $\tilde{O}(\mathcal{S}_{\text{Tr}}(B, \epsilon))$ samples of the Gibbs state $\rho^{(t)} = \frac{W^{(t)}}{\text{Tr}[W^{(t)}]}$ by Definition 2;
- 4 Using these $\tilde{O}(\mathcal{S}_{\text{Tr}}(B, \epsilon))$ copies of $\rho^{(t)}$, search for a $j^{(t)} \in [m]$ such that $\text{Tr}(A_{j^{(t)}} \rho^{(t)}) > a_{j^{(t)}} + \epsilon$ by Lemma 3 with $\delta = \frac{\epsilon^2}{400 \ln n}$. Take $M^{(t)} = \frac{1}{2}(I_n - A_{j^{(t)}})$ if such $j^{(t)}$ is found; otherwise, claim that $\mathcal{S}_\epsilon \neq \emptyset$ (the SDP is feasible);
- 5 Define the new weight matrix: $W^{(t+1)} = \exp[-\frac{\epsilon}{2} \sum_{\tau=1}^t M^{(\tau)}]$;
- 6 Claim that $\mathcal{S}_0 = \emptyset$ and terminate the algorithm.

Brandao *et al*, arXiv:1710.02581 (2017)

Universal quantum emulation



Marvian & Lloyd, arXiv: 1606.02734 (2016)



Programming parity can be restored to quantum computing using the **Density Matrix Exponentiation algorithm**

We demonstrated a proof of principle version of this algorithm using superconducting qubits, and a novel gate construction for approximately resetting a known state

More details: www.arXiv.org/abs/2001.08838



Cirq



Labber
QUANTUM



Mollie Schwartz
Lincoln Lab



Ami Greene
MIT



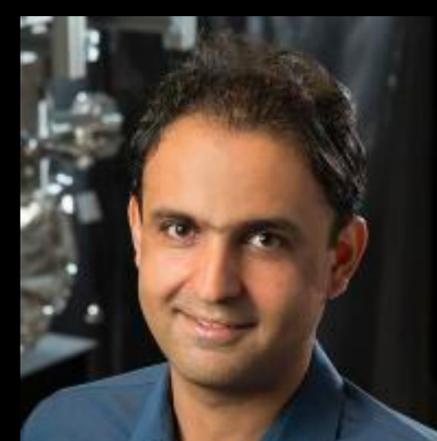
Gabriel Samach
MIT/Lincoln Lab



Andreas Bengtsson
Chalmers/Google



Chris McNally
MIT

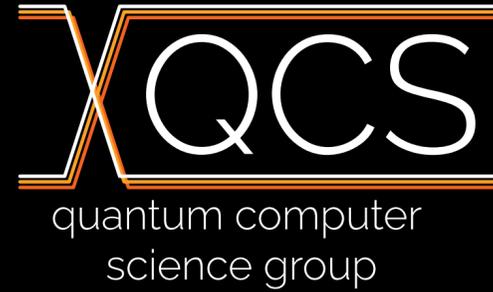


Iman Marvian
Duke



Will Oliver
MIT

Superconducting quantum computing in Denmark



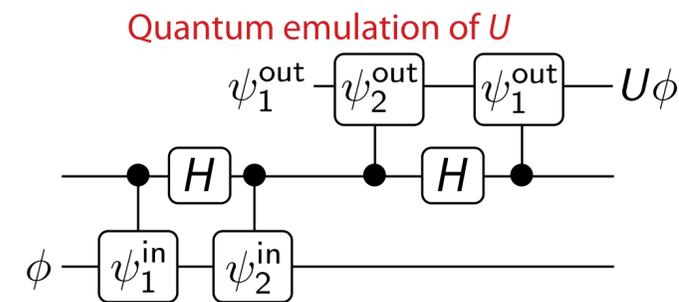
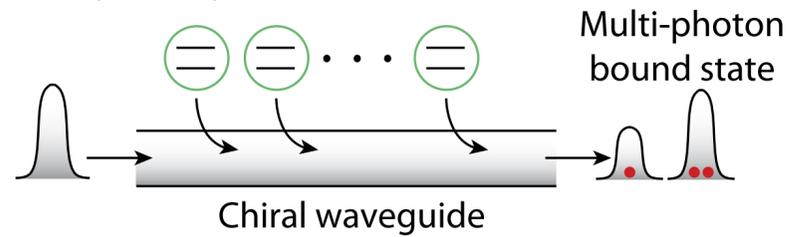
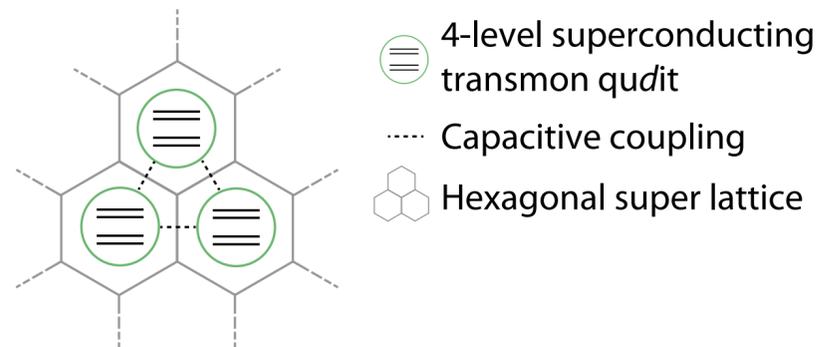
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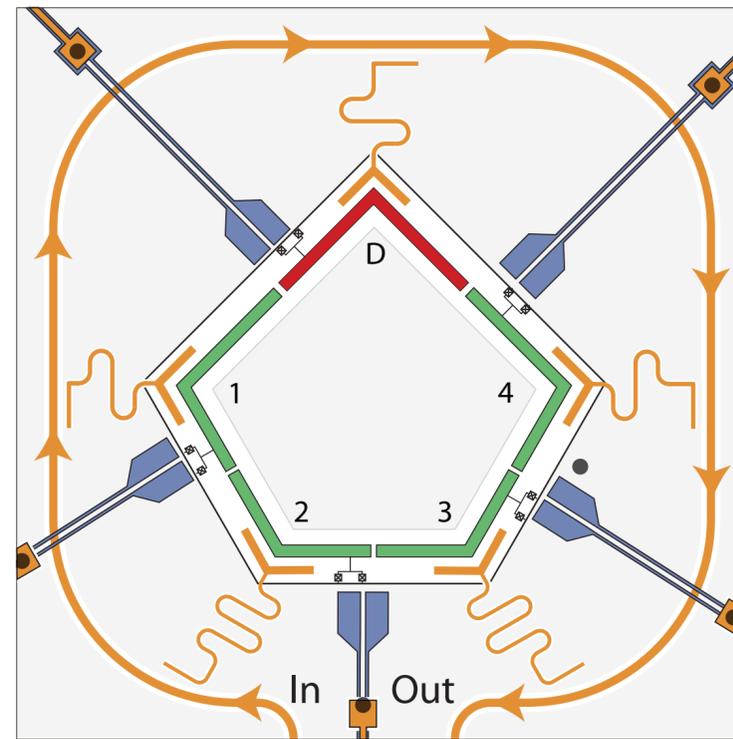
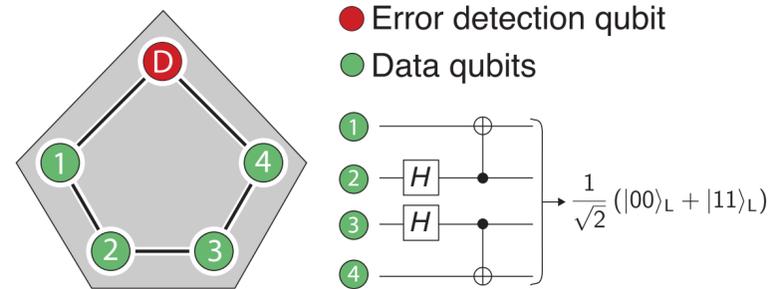
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COPENHAGEN



Quantum algorithms and simulation

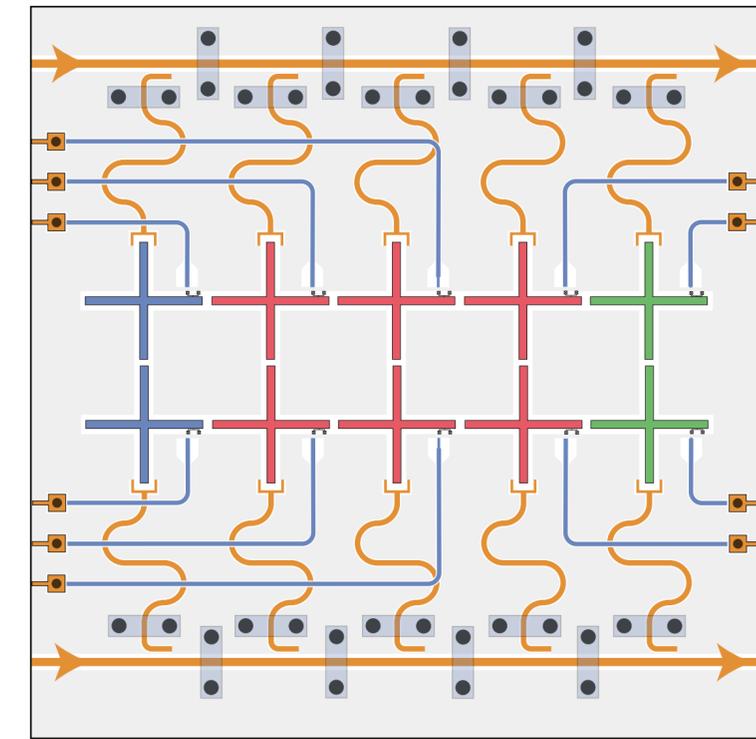
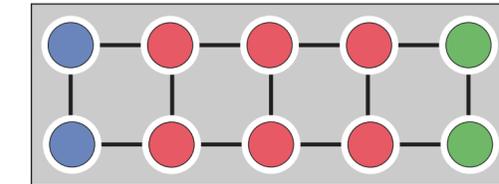


Quantum fault tolerance



On-chip quantum communication protocols

Alice Noisy channel Bob



Want to study foundational problems and applications of superconducting qubits to quantum information processing?
We are looking for students and postdocs! [Let me know at mkjaergaard@nbi.ku.dk](mailto:mkjaergaard@nbi.ku.dk)